

Unit 1:
A CDE 1

one variable multi-step
both sided equations

Objective:

Students will be able to:

- solve equations by getting all variables on the same side of the equation.
- write and justify appropriate properties to steps.

Addition and Multiplication Properties

Distribution Property:

$$a(b + c) = ab + ac$$

Example:

$$\begin{aligned} 6(7 + 8) &= 6 \cdot 7 + 6 \cdot 8 \\ &= 42 + 48 \\ &= 90 \end{aligned}$$

Words to Remember

Commutative property of addition

$$a + b = b + a$$

Example: $6 + 7 = 7 + 6$

Associative property of addition

$$(a + b) + c = a + (b + c)$$

Example: $(6 + 7) + 8 = 6 + (7 + 8)$

Identity property of addition

$$a + 0 = a$$

Example: $8 + 0 = 8$

Inverse property of addition

$$a + (-a) = 0$$

Example: $8 + (-8) = 0$

Commutative property of multiplication

$$ab = ba$$

Example: $6 \cdot 7 = 7 \cdot 6$

Associative property of multiplication

$$(ab)c = a(bc)$$

Example: $(6 \cdot 7)8 = 6(7 \cdot 8)$

Identity property of multiplication

$$a \cdot 1 = a$$

Example: $8 \cdot 1 = 8$

Inverse property of multiplication

$$a \cdot \frac{1}{a} = 1$$

Example: $8 \cdot \frac{1}{8} = 1$

Properties of Equality

These properties allow us to balance and solve equations involving real numbers.

ex/

$$\begin{aligned} (+) \text{ prop. } (\Rightarrow) \\ (*) \text{ prop. } (\Rightarrow) \end{aligned}$$

Properties of addition and Multiplication

These properties are the definition of how numbers should behave.

ex/

$$\begin{aligned} 3 + 4 &= 7 \\ 4 + 3 &= 7 \\ 5 \cdot 2 &= 10 \\ 2 \cdot 5 &= 10 \end{aligned}$$

1 Example

$$6m + 5 - 7m = 10 - 5m + 3 \quad \text{Steps/Reason}$$

① $-m + 5 = 13 - 5m$	① Combine like terms
② $+5m$	② $(+)$ prop. (\Rightarrow)
$4m + 5 = 13$	
③ -5	③ $(-)$ prop. (\Rightarrow)
$4m = 8$	
④ $\frac{4m}{4} = \frac{8}{4}$	④ (\div) prop. (\Rightarrow)
$m = 2$	

2 Example

$$8w + 4 - 2w = w + 1$$

Steps/Reason

①	$6w + 4 = w + 1$	① Combine like terms
②	$\frac{6w + 4}{+4} = \frac{w + 1}{-4}$	② \ominus prop \ominus
③	$6w = w - 3$ $\frac{-w}{-w} \quad \frac{-w}{-w}$	③ \ominus prop \ominus
④	$5w = -3$ $\frac{5w}{5} = \frac{-3}{5}$	④ \div prop. \ominus
	$w = \frac{-3}{5}$	

3 Example

$$3(n-2) - 1 = 2 - 5(n+5)$$

Steps/Reason

①	$3n - 6 - 1 = 2 - 5n - 25$	① Distributive prop.
②	$3n - 7 = -23 - 5n$	② Combine like terms.
③	$\frac{+7}{+7} \quad \frac{+7}{+7}$	③ \oplus prop. \ominus
④	$3n = -16 - 5n$ $\frac{+5n}{+5n} \quad \frac{+5n}{+5n}$	④ \oplus prop. \ominus
⑤	$\frac{8n}{8} = \frac{-16}{8}$	⑤ \div prop. \ominus
	$n = -2$	

Quiz Corrections

Problem

Correction

Reason

#2 $y - y_1 = m(x - x_1)$ $\begin{matrix} x & y & x & y \\ (5, -1) & (-3, 2) \end{matrix}$

$$y + 1 = \frac{2 + 1}{-3 - 5} (x - 5)$$

$$y + 1 = -\frac{3}{8} (x - 5) = -\frac{3}{8}x + 5 \frac{15}{8}$$

$$y + 1 = \frac{3}{8}x + \frac{15}{8}$$

$$\boxed{y = \frac{3}{8}x + \frac{7}{8}}$$

$$\begin{matrix} \frac{15}{8} & - & \frac{1}{1} & \frac{8}{8} \\ & & \vee & \\ & & \frac{7}{8} & \end{matrix}$$

The reason I got this wrong was because I forgot how to distribute the $-\frac{3}{8}$ to the -5 so then when I moved the $+1$ over it was all wrong.



#4

$y - y_1 = m(x - x_1)$ $m(x) = 1\left(\frac{2}{5}x\right)$

$\begin{matrix} x & y \\ (2, -3) \end{matrix}$ \downarrow

$$y + 3 = \frac{5}{2} (x - 2)$$

$$m = \frac{5}{2}$$

$$y + 3 = \frac{5}{2}x - \frac{10}{2}$$

$$-\frac{10}{2} \quad -\frac{3}{1} \quad \frac{4}{2}$$

$$-\frac{16}{2} \quad -\frac{8}{1} = -8$$

$$\boxed{y = \frac{5}{2}x - 8}$$

The 1 threw me off when I only needed the m and coordinates. Then I had to use the point-slope formula but I didn't use it.

#5a

if $a=0$ then it would lie on the y -axis, if the $b=0$ then it would lie on the x -axis, so false.

I thought that this meant $(0,0)$ so I was thinking it was the origin but I had to think about each one differently.

#5c

The slope is actually defined because the y would be part of $y = mx + b$

I got this wrong because I thought it was just a line at first but I was wrong