

Example

Decompose the function: That is, find two functions f and g , such that: $h(x) = f(g(x))$ where none are the $y=x$.

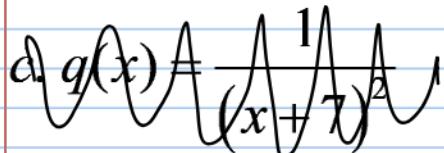
a. $h(x) = \sqrt{x+2} + 6$

a) $f(x) = x + 6$ $g(x) = \sqrt{x+2}$ or //

$g(x) = x+2$

$f(x) = \sqrt{x+6}$

b. $p(x) = (x+1)^2 - x - 1$



b) $f(x) = x - 1$

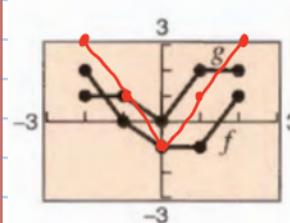
$g(x) = (x+1)^2 - x$

or // $f(x) = x^2 - x$

$g(x) = x+1$

Example

Use the graph to graph $h(x) = f(x) + g(x)$

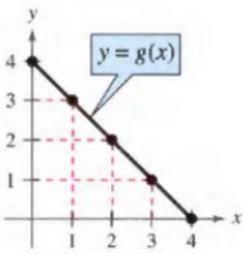
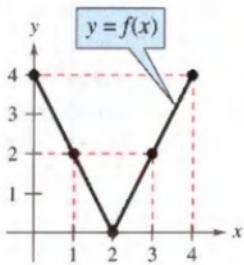


x	$h(x)$
2	3
1	1
0	$-1+0 = -1$
-1	$0+1 = 1$
-2	3

$$\begin{aligned}h(2) &= f(2) + g(2) & h(1) &= f(1) + g(1) \\&= 1 + 2 &&= -1 + 2 \\&\Rightarrow 3 &&\Rightarrow 1\end{aligned}$$

Example

Use the graph to evaluate the functions



a. $f(1) + g(1) = 5$

b. $(f \circ g)(2) = f(g(2)) = f(2) = 0$

c. $(f \cdot g)(3) = f(3) \cdot g(3) = 2(1) = 2$

d. $\frac{f(4)}{g(4)} = \frac{4}{0} = \text{undefined}$

Error Analysis

A student found the product of two functions.

Given $f(x) = 3x^2 + x - 8$ and $g(x) = x - 1$.

Solution:

$$\begin{aligned}f(x) \cdot g(x) &= (3x^2 + x - 8)(x - 1) = \\&= 3x^3 + x^2 - 8x - 3x^2 - x + 8 \\&= 3x^3 - 4x^2 - 9x + 8\end{aligned}$$

The answer is $3x^3 - 4x^2 - 9x + 8$.

What is the error? Explain how to solve the problem correctly.